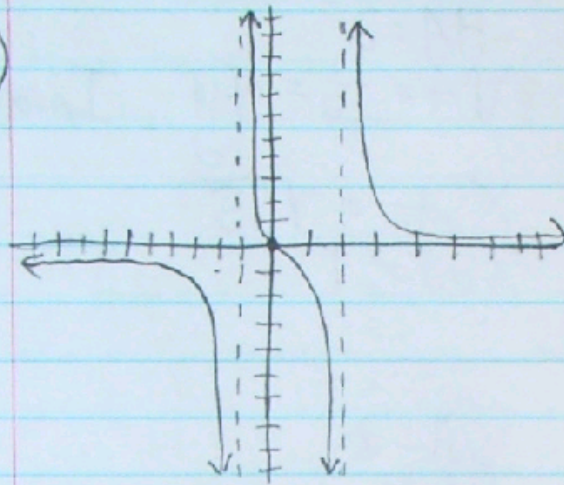


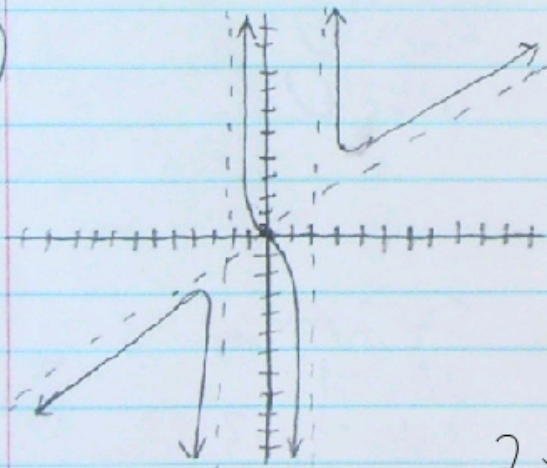
a.)



$$\begin{aligned} HA &= 0 \\ VA &= -1, 2 \\ X_{int} &= 0 \\ Y_{int} &= 0 \end{aligned}$$

$$f(x) = \frac{3x}{x^2 - x - 2}$$

b.)



$$\begin{aligned} SA &= .5x \\ VA &= -2, 2 \\ HA &= \text{Non-existent} \\ X_{int} &= 0 \\ Y_{int} &= 0 \end{aligned}$$

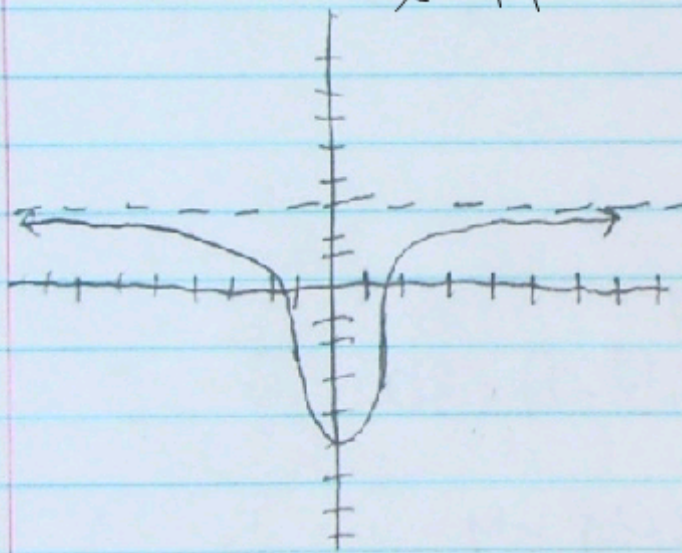
$$f(x) = \frac{x^3}{2x^2 - 8}$$

$$2x^2 + 0x - 8 \overline{) \begin{array}{r} x^3 + 0x^2 + 0x + 0 \\ x^3 + 0x^2 - 4x \\ \hline 4x + 0 \end{array}}$$

$\frac{1}{2}x + \frac{4}{2x^2 - 8}$

$$f(x) = \frac{3x^2 + x - 5}{x^2 + 1}$$

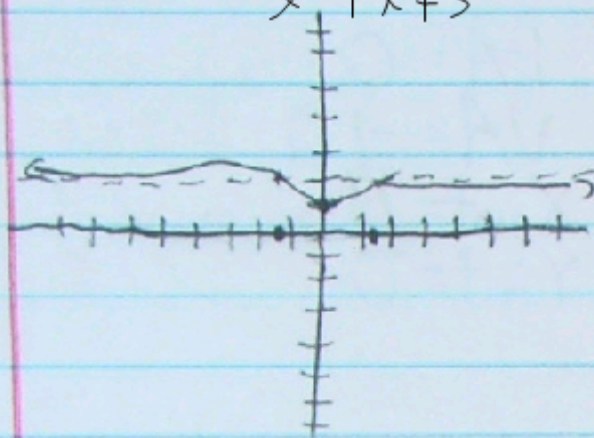
c.



$$\begin{aligned} HA &= 3 \\ VA &= j, j - \text{No vert. asympt} \\ X_{\text{int}} &= -\frac{1}{6} \pm \frac{\sqrt{61}}{6} \\ Y_{\text{int}} &= -5 \end{aligned}$$

$$f(x) = \frac{2x^2 + 3}{x^2 + x + 3}$$

d.)

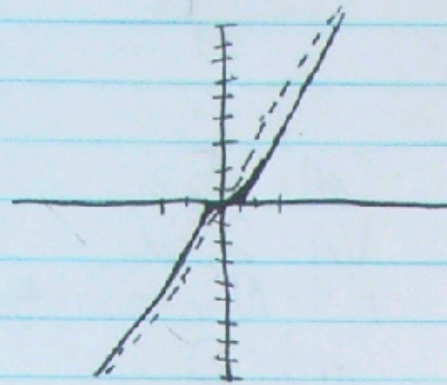


$$\begin{aligned} HA &= 2 \\ VA &= -\frac{1}{2} \pm \frac{\sqrt{11}}{2} = \text{Imaginary} \\ X_{\text{int}} &= \pm \sqrt{1.5} \\ Y_{\text{int}} &= 1 \end{aligned}$$

No
vert.
asympt.

$$f(x) = \frac{2x^3}{x^2+1}$$

e)

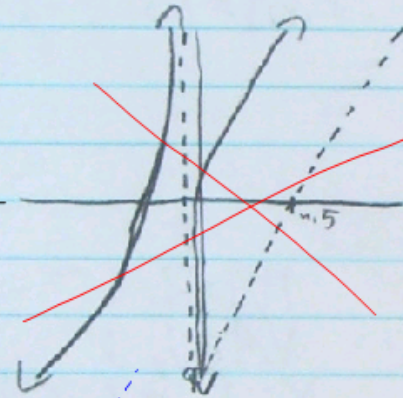


$$\begin{aligned} SA &= 2x \\ VA &= i, -i \\ x_{int} &= 0 \\ y_{int} &= 0 \end{aligned}$$

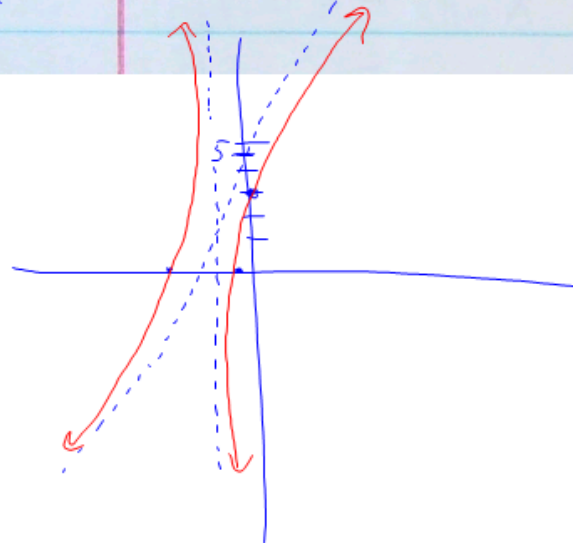
f)

$$f(x) = \frac{2x^2 + 7x + 3}{x+1}$$

$$(2x+1)(x+3)$$

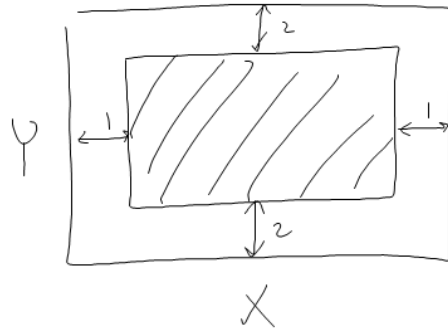


$$\begin{aligned} SA &= 2x - 9 \\ VA &= -1 \\ x_{int} &= -\frac{1}{2}, -3 \\ y_{int} &= 3 \end{aligned}$$



$$\begin{aligned} & \frac{2x+5}{x+1} + \frac{-2}{x+1} \\ & x+1 \overline{) 2x^2 + 7x + 3} \\ & \quad \underline{2x^2 + 2x} \quad \\ & \quad \quad 5x + 3 \\ & \quad \quad \underline{5x + 5} \\ & \quad \quad \quad -2 \end{aligned}$$

Station 7



$$30 = (x-2)(y-4)$$

$$\frac{30}{x-2} = y-4$$

$$\frac{30}{x-2} = y-4$$

$$y = \frac{30}{x-2} + 4 \frac{(x-2)}{x-2}$$

$$y = \frac{30 + 4(x-2)}{x-2}$$

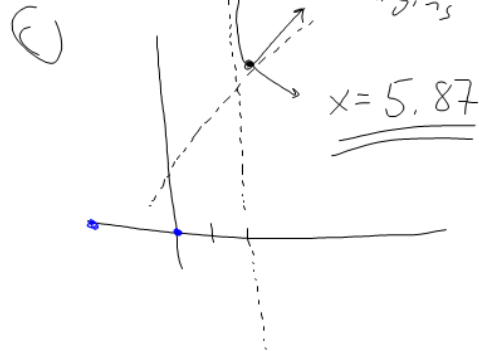
$$y = \frac{30 + 4x - 8}{x-2}$$

$$y = \frac{4x + 22}{x-2}$$

$$A = x \left(\frac{4x + 22}{x-2} \right)$$

$$A = \frac{4x^2 + 22x}{x-2}$$

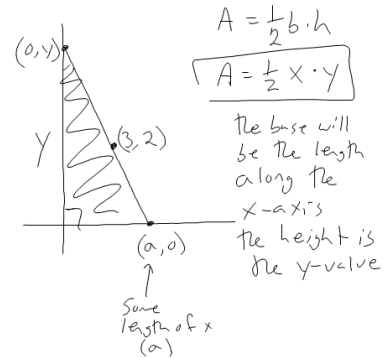
(b) Domain $x > 2$
because of margins



slant $x-2$ $\overline{4x^2 + 22x}$

$$\begin{array}{r} 4x^2 + 22x \\ 4x^2 - 8x \\ \hline 30x + 0 \\ 24x - 60 \\ \hline 6x + 60 \end{array}$$

Station 8



We need to find an equation to link x + y
 use the point slope form for the line

$$y = m(x - x_1) + y_1$$

so we need to find m first

To find m use $(3, 2)$ $(x, 0)$. But since we have an x for our independent variable already, let's use the letter " a " to denote the specific x -value. So our points are $(3, 2)$ and $(a, 0)$. The slope is then $m = \frac{2-0}{3-a} = \frac{2}{3-a}$ and we can put that back into the point slope equation using the point $(a, 0)$ which is what we ultimately want to find.
 $y = \frac{2}{3-a}(x-a) + 0$ or $y = \frac{2}{3-a}(x-a)$

Now plug back into the original equation $A = \frac{1}{2}xy$ using what we just found as the y , and " a " for x to stay consistent
 $A = \frac{1}{2}a \left(\frac{2(x-a)}{3-a} \right)$. Now the key is

that the height or y -value corresponds to an x -value of zero so we have

$$A = \frac{1}{2}a \left(\frac{2(0-a)}{3-a} \right)$$

$$A = \frac{1}{2}a \left(\frac{-2a}{3-a} \right)$$

$$A = \frac{-a^2}{3-a} \quad \text{or} \quad \frac{a^2}{a-3}$$

Graphing we find the minimum value for A is 12 when $a=6$.

Test - No Calc.

→ 3 problems like station 6

- Vert. Asympt.
- Horiz. Asympt.
- Slant Asympt.
- x-int.
- y-int.
- holes

→ 2 application problem